An evaluation of string similarity measures on pricelists of computer components

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Toner pro LaserJet 4/4M, 4/4M Plus, 5/5N/5M (8800)

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Logitech myš Pilot Optical Mouse Black, USB/PS/2, retail

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- Some suppliers provide also part number for some components. It should be unique.
- Part numbers provide a very reliable matching.
- Unfortunatelly, many items in pricelists do not have any part number assigned.

• As a reference method we used the fulltext search of MySQL: http://dev.mysql.com/doc/refman/5.0/en/ fulltext-search.html

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• We denote the similarity value of two strings S<sub>1</sub> and S<sub>2</sub> provided by this fulltext search method as Sim<sub>1</sub>(S<sub>1</sub>, S<sub>2</sub>).

• This method is described in detail in our previous paper on this topic, which is part of the proceedings of the Eighth Czech-Japan Seminar in 2005.

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- We measure the similarity  $Sim(S_1, S_2)$  of two strings  $S_1, S_2$  by the total length of substrings of  $S_1$  that are substrings of string  $S_2$ .

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- In the experiments we used the relative string similarity defined as

$$Sim_2(S_1, S_2) = \frac{Sim(S_1, S_2)}{Sim(S_1, S_1)}$$

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#### Example



# $\begin{array}{c|c} R_2 \\ \hline W & I & N & T & R & M & N \\ \hline \end{array}$

# Example



 $Similarity(R_1, R_2) = 0$ 

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Similarity  $(R_1, R_2) = 2$ 

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 $Similarity(R_1, R_2) = 2 + 3$ 

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#### Example



 $Similarity(R_1, R_2) = 2 + 3$ 

# Example $R_{1}$ $W \parallel N \square O W S \square T \blacksquare R M$ $R_{2}$ $W \parallel N \square T R M N \blacksquare$

$$k = 2$$
  
 $R = "IN"$   
Length(R) = 2

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*Similarity*( $R_1, R_2$ ) = 2 + 3 + 2

#### Example



*Similarity*( $R_1, R_2$ ) = 2 + 3 + 2

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#### Example



*Similarity*( $R_1, R_2$ ) = 2 + 3 + 2

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#### Example



Similarity  $(R_1, R_2) = 2 + 3 + 2 + 2$ 

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#### Example



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Similarity  $(R_1, R_2) = 2 + 3 + 2 + 2$ 

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#### Example



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Similarity  $(R_1, R_2) = 2 + 3 + 2 + 2 + 2 = 11$ 

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- m(x) be the number of strings containing token x.
- The weight of a token x in string S is defined as

$$w(x,S) = \frac{n(x,S)}{n(S)} \log \frac{m}{m(x)}$$

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 Similarity of two strings S<sub>1</sub> and S<sub>2</sub> is then computed as the scalar product of normalized weight vectors v(S<sub>1</sub>) and v(S<sub>2</sub>)

$$Sim_3(S_1, S_2) = \sum_{i=1}^d v(x_i, S_1) \cdot v(x_i, S_2) = \mathbf{v}(S_1)^T \cdot \mathbf{v}(S_2)$$
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 Note that since both vectors are sparse the computation of the scalar product can be efficiently implemented.

#### Example

 $S_1$  toner\_magenta\_pro\_clp-510/510n,\_az\_5000\_stran

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- $S_1$  toner\_magenta\_pro\_clp-510/510n,\_az\_5000\_stran
- S<sub>2</sub> samsung\_toner\_magenta\_pro\_clp510/n\_(5000str\_)

#### Example

- $S_1$  toner\_magenta\_pro\_clp-510/510n,\_az\_5000\_stran
- S<sub>2</sub> samsung\_toner\_magenta\_pro\_clp510/n\_(5000str\_)
  - For simplicity assume tokens from these two strings only: toner, magenta, pro, clp, 510, 510n, az, 5000, stran, samsung, clp510, n, 5000str

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#### Example

- $S_1$  toner\_magenta\_pro\_clp-510/510n,\_az\_5000\_stran
- S<sub>2</sub> samsung\_toner\_magenta\_pro\_clp510/n\_(5000str\_)
  - For simplicity assume tokens from these two strings only: toner, magenta, pro, clp, 510, 510n, az, 5000, stran, samsung, clp510, n, 5000str

•  $w(\texttt{toner}, S_1) = \frac{1}{9} \log \frac{36478}{274} = 0.236$ 

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- $w(\texttt{toner}, S_1) = \frac{1}{9} \log \frac{36478}{274} = 0.236$
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- $w(\text{magenta}, S_1) = \frac{1}{9} \log \frac{36478}{59} = 0.310$
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  - For simplicity assume tokens from these two strings only: toner, magenta, pro, clp, 510, 510n, az, 5000, stran, samsung, clp510, n, 5000str
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  - $\mathbf{w}(S_1) = (0.236, 0.310, 0.285, 0.420, 0.235, 0.345, 0.034, 0.121, 0.097, 0.000, 0.000, 0.000, 0.000)$

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  - $\mathbf{w}(S_2) = (0.303, 0.399, 0.366, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.056, 0.451, 0.023, 0.456)$

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$$\mathbf{v}(S_1) = \frac{\mathbf{w}(S_1)}{\sqrt{\sum_{i=1}^d w(x_i, S_1)^2}} = \frac{\mathbf{w}(S_1)}{0.780}$$

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•  $\mathbf{v}(S_1) = (0.302, 0.397, 0.365, 0.538, 0.301, 0.442, 0.044, 0.155, 0.124, 0.000, 0.000, 0.000, 0.000)$ 

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- $\mathbf{v}(S_2) = (0.339, 0.446, 0.409, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.063, 0.504, 0.026, 0.510)$

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V(S<sub>1</sub>) = (0.302, 0.397, 0.365, 0.538, 0.301, 0.442, 0.044, 0.155, 0.124, 0.000, 0.000, 0.000)
 V(S<sub>2</sub>) = (0.339, 0.446, 0.409, 0.000, 0.000, 0.000, 0.000, 0.000, 0.000, 0.003, 0.504, 0.026, 0.510)

 $Sim_3(S_1, S_2) = \mathbf{v}(S_1)^T \cdot \mathbf{v}(S_2)$  $= 0.302 \cdot 0.339 + 0.397 \cdot 0.446 + 0.365 \cdot 0.409 = 0.429$ 

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 $Sim_4(S_1, S_2) = c_1 \cdot Sim_1(S_1, S_2) + c_2 \cdot Sim_2(S_1, S_2) + c_3 \cdot Sim_3(S_1, S_2)$ 

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where  $\mathbf{c} = (c_1, c_2, c_3)$  was set to (0.3, 1, 1), (0, 1, 1), and (0, 1, 2).

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• We selected two pricelists of computer components from two different suppliers.

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- Then we checked whether the component with the same part number is among those *k* selected ones.
- We counted the number of these cases and computed the relative success rate for each method with respect to k.

# Results of experiments



Example (Acer server)

AAG320 PD 940 (3.2 GHz, 2x 2MB, 800 MHz FSB), 1x 512 MB DDR2 533/16x DVD-ROM Acer Altos G320-PD940 3.2GHz/2x2MB,800F/512MB/DVD/noHDD/noKB

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- Whether a symbol is a separator depends on its context.
- For example, the space symbol is a separator between PD940 and 3.2 GHz but "3.2 GHz" should be one token.

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Example (Ink cartridge)

Ink. náplň No. 84 pro DesignJet 10PS/20PS/50PS C5016A Black ink Cartridge pro DSJ x0ps

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#### Example (Cable)

Kabel Pure AV Blue series Firewire 4pin/6pin, 1.8m PureAV kabel FireWire, 4/6 kolíků - 1,8 m - Řada Blue

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Example (Mail antispam and antivirus)

SYMANTEC BRIGHTMAIL ANTISPAM + ANTIV 6.0 SUBS + GOLD MAINT 1YR IN VALUE BAND F(5 Sym. Bright.Antispam + Antivirus 6.0 IN F(500-999) + 1YR GM

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• GM is an abbreviation for GOLD MAINT.

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• a smarter method for separating strings into tokens

- We performed experiments with three string similarity measures on real data
- We observed the best performance for the vector based method.
- At 62% of cases found the correct component first and in 83% of cases it was among the first five.
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- a smarter method for separating strings into tokens
- the vector method as a basis for further improvements

#### Future work

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Since the matrix P and vectors v(S<sub>1</sub>), v(S<sub>2</sub>) are sparse the computations can be efficiently implemented.